



Balancing of cost-oriented U-type general resource-constrained assembly line: new constraint programming models

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Abstract

In simple assembly line balancing problems, it is assumed that the resources required to perform the tasks are available at the relevant station for task assignment. However, each task may need different resource types depending on the difficulty, complexity and technical requirements of the tasks in real life. For this reason, tasks and resources belonging to these tasks must be assigned to the relevant station while balancing the line. In this study, the resource-constrained U-shaped assembly line balancing problem (U-GRCALBP) is discussed. According to the literature research, there is no study dealing with U-GRCALBP. Two different constraint programming (CP) models that define the resource constraints as “and/or” constraint types with concurrent resource types have been developed. In these models, the sum of resource usage costs and station opening cost minimization is aimed. The models are explained with an illustrative example and the efficiency of the models is tested by deriving new resource constraints on five different data set each taking into account four different cycle times and the number of two and four resource types. The number of stations obtained, the total number of resources used, total station opening and resource usage costs, and CPU time are used as performance criteria. The results are compared with the traditional U-type assembly line balancing problem results. The proposed CP models give superior performance on all data sets, especially in terms of total cost. The numerical results show that both CP models are effective in solving the problem. Furthermore, some managerial implications are presented to be useful for professionals, organizations, and society.

Keywords Assembly line balancing · U-type · General resource constraints · Conjunctive constraints · Constraint programming

1 Introduction

The products had to be produced in high quantities but economically due to the increasing demand. One of the production systems established to produce products more economically is assembly lines. The assembly line consists of sequential workstations connected to each other by a transport system in a specified area. The assigned tasks are fulfilled at these stations and the main product is obtained

by assembling the sub-parts of the product. The assembly lines, which were first established by Henry Ford, are now used to produce many products such as automobiles, white goods, furniture, etc.

Different types of assembly lines have emerged due to changes in their features, such as layout type, number of models, and task time variability. Assembly lines are classified as simple or straight lines and U-lines according to the layout type. While the stations are arranged in a row on straight lines, in U-type lines, the stations have a layout arrangement in the form of the letter U. U-type lines have been preferred in practice due to the following situations: (i) Failure to establish a straight line due to space constraints, (ii) to reduce cycle time (i.e., to increase line efficiency), (iii) to reduce performance degradation due to monotony in employees, (iv) Significantly increasing the production output rate by the Just in Time (JIT) principle.

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The contribution of U-type lines to JIT systems can be given as increasing production flexibility, improving communication between stations, and facilitating operator mobility between stations. Since the assembly line is formed in a U shape, the beginning and end of the line are aligned. The fact that the tasks to be performed will be performed on either side of the U-type line allows more task assignment alternatives to be evaluated and more efficient lines to be established (Eghtesadifard et al. 2020).

Assembly line balancing problems (ALBP) are the problem of assigning tasks to the station where the tasks will be performed under the desired constraints in all types of assembly lines. In ALBP, a combinatorial NP-hard problem, while trying to optimize one or more objectives, priority relations, task assignment, and station cycle time constraints, should also be provided. However, in practice, besides these basic constraints, some specific constraints arising from the sectorial conditions and the technical characteristics of the tasks to be performed at the stations can also be taken into account. In the literature, these constraints are classified as assignment constraints, resource constraints, and distance constraints (Pınarbaşı et al. 2019). Assembly lines, resources are defined as human and/or machine. The number or cost of these resources is also taken into account in ALBP. Such problems are called resource-constrained assembly line balancing problem (RCALBP). RCALBP was first addressed by Ağpak and Gökçen (2005), and a mathematical model for the problem was proposed. It is ensured that the tasks that need the same resources in their work are assigned together. In this way, it is aimed to balance the line and use fewer resources.

In the literature, it is seen that exact and heuristic solution approaches are frequently used for the solution of ALBP (Sivasankaran and Shahabudeen 2014). Exact solution methods are methods by which the optimum solution to the problem can be obtained. Examples of these methods are mathematical modeling, constraint programming, and branch-bound algorithm. Examples of heuristic solution approaches are genetic algorithm, taboo search, ant colony, annealing simulation, and problem-specific heuristics. In the problem addressed in this study, alternative and different numbers of resources are needed. In this case, it requires logical constraints in the modeling of the problem. The constraint programming method is preferred in the solution of the problem because it provides exact solutions and allows the constraints in different structures such as mathematical, logical, linguistic, etc., to be defined easily. Constraint programming, which is a preferred method in solving combinatorial problems, has been widely used in ALBP solutions in recent years. It is seen as a result of the studies that it is an effective method in ALBP solution.

In this study, the U-type general resource-constrained assembly line balancing problem (U-GRCALBP) is discussed. The aim of the study is to minimize the resource cost due to the resource used and the stations opening cost. The constraint programming approach is used as a solution method. Two different constraint programming models have been proposed to solve the problem. New resource constraints are generated for problem sets in the literature to test the proposed models' performance. The results showed that constraint programming is effective in solving U-GRCALBP.

The main contributions of this study can be listed as follows: (1) The U-type resource-constrained problem is addressed for the first time, (2) The constraint programming solution approach, which is an exact method, has been used for the solution of the problem, (3) The tasks are performed with different types and numbers of alternative resources in this problem type. (4) Resource constraints are defined as general resource constraints in the "and/or" structure. (5) It has been shown that CP is an effective solution method in solving U-GRCALBP.

This paper is organized as follows. Section 1 is related to the introduction. In Sect. 2, studies using both resource-constrained ALBP and constraint programming in the ALBP solution are given in comparative tables. In the third chapter, the RCALBP problem is defined, and the assumptions of the problem discussed are also included. In the fourth chapter, two CP models proposed for the solution of the problem are given. In the fifth chapter, an illustrative example solution is explained with the suggested models. In the sixth chapter, the numerical experiments performed to test the models' performance are included and the comparative results of the experiments are presented. In the seventh section, the results of the study and recommendations for future studies are given.

2 Literature review

Since the ALBP literature is quite extensive, the literature to be given in the study has been compiled to include RCALBP studies. There are not many studies about RCALBP in the literature. Studies classified according to the results of the literature review are summarized in Table 1. In the classification of the studies, the following features of ALBP are taken into consideration: line shape, resource type, objective function, resource constraint type, and solution method. The literature will be explained in the order of this classification.

The studies have been handled in three different ways in terms of line shape: straight, U-shape, and two-side. When the results given in Table 1 are examined, it is seen that most work (i.e., 17 pieces of work) is done for straight

Table 1 The studies about RCALBP in the literature

Studies	Line shape		Resource type		Objective function							Resource constraint type			Solution method	
	Straight	U-shape	Two-sided	Simple case	General case	Ns	Nr	Ec	E	Tw	Rc	C	Tc	Resource constraint type		
														Dedicated		Alternative
Ağpak and Gökçen (2005)	•			•		•	•							•		MP
Kao et al. (2010)	•			•		•	•							•		SRA
Kao et al. (2011)	•			•		•	•							•		RPWBH
Corominas et al. (2011)	•				•	•	•							•	•	MP
Chen et al. (2012)	•			•		•	•					•				GA
Mete and Agpak (2013)			•		•	•	•							•		MP
Ogan and Azizoglu (2015)		•		•				•					•			MP & BB
Jusop and Ab Rashid (2017)	•			•		•			•				•			GA
Quyen et al.(2017)	•			•		•	•						•			GA
Kamarudin and Ab. Rashid (2017)	•			•		•	•						•			GA
Chen et al.(2018)	•			•		•	•			•				•		GA
Pereira (2018)	•				•					•	•			•		MP
Khalib et al. (2019)	•			•		•	•							•		GA
Alakas et al. (2020)	•			•		•	•					•		•		CP
Alakaş (2021)	•				•							•		•	•	CP
Leiber and Reinhart (2021)	•			•								•				GA
Leiber et al. (2021)	•			•									•			GA
Jin et al. (2022)	•				•							•		•	•	WOA
Michels and Costa (2022)	•			•			•					•		•		MP
This study		✓			✓								✓	✓	✓	CP

Ns number of stations, Nr number of resources, Ec total equipment cost, E efficiency, Tw total workforce, Rc resource cost, C cycle time, Tc total cost, CP constraint programming, GA genetic algorithm, MP mathematical programming, SRA shortest route algorithm, RPWBH rank positional weight-based heuristic, BB branch and bound, WOA whale optimization algorithm

assembly lines. There is only one study for each U-shape (Ogan and Azizoglu 2015) and two-sided (Mete and Agpak 2013) RCALBP. All the results of these assessments, studies taking into account U-type RCALBP are still insufficient.

Studies can be classified into two groups as simple and general cases according to resource types. There are many studies (i.e., 14 pieces) for the simple case RCALBP in the literature. There are only five studies (Corominas et al. 2011; Mete and Agpak 2013; Pereira 2018; Alakaş 2021; Jin et al. 2022) for general case RCALBP (Table 1). According to the literature research, there is still a gap in the literature for the solution of ALBP with general resource constraints.

When the literature studies in Table 1 are examined in terms of the objective function, it is determined that the studies use eight different objective functions. It is seen that the literature studies mostly consider the minimization of the number of stations (Ns) and the minimization of the number of resources (Nr) as objective functions. In addition to these, in the literature, total equipment cost (Ogan and Azizoglu 2015), line efficiency maximization (Jusop and Ab Rashid 2017), total workforce balancing (Pereira 2018; Chen et al. 2018), resource cost minimization (Pereira 2018), cycle time minimization (Chen et al. 2012; Alakas et al. 2020) have been considered as objective functions. A result seen in Table 1 is that the problem is mostly considered as a multi-objective in the studies. Usually, the minimization of the number of stations and the number of resources simultaneously is considered together. In addition to these, there are also studies that consider total workforce and resource cost together (Pereira 2018) and the number of resources and cycle time minimization together (Alakas et al. 2020). There are two studies (Mete and Agpak 2013; Leiber et al. 2021) considering the total cost function expressed as the sum of the resource cost used and the station opening cost. Leiber and Reinhart (2021) consider acquisition cost and positioning costs of resources in line balancing after assigning the task and selecting resource types.

Studies in the literature are classified into three different groups regarding resource constraint type as dedicated, alternative, and concurrent. According to the studies summarized in Table 1, the most considered resource constraint is the dedicated type (i.e., 14 works). In only three studies (Ağpak and Gökçen 2005; Alakas et al. 2020; Michels and Costa 2022), the alternative resource type has been considered together with the dedicated resource type. Four studies (Corominas et al. 2011; Mete and Agpak 2013; Alakaş 2021; Jin et al. 2022) can be given as an example of the concurrent resource type. As a result, studies considering alternative and concurrent resource types are still insufficient in the literature.

When RCALBP studies are evaluated in terms of solution method, it is seen that exact (e.g., MP, CP), heuristic (e.g., SRA), and meta-heuristic (e.g., GA) solution methods exist. According to the results specified in Table 1, the most used solution method in the RCALBP solution is the genetic algorithm (Chen et al. 2012, 2018; Jusop and Ab Rashid 2017; Kamarudin and Ab. Rashid 2017; Quyen et al. 2017; Khalib et al. 2019; Leiber and Reinhart 2021; Leiber et al. 2021). Ağpak and Gökçen (2005) is the first study to use the exact method in solving the problem. Also, the studies using the mathematical model as a solution method can be given as an example (Corominas et al. 2011; Mete and Agpak 2013; Ogan and Azizoglu 2015; Pereira 2018; Michels and Costa 2022). It is possible to list the heuristic algorithms used in the solution of the problem as follows: shortest route algorithm (Kao et al. 2010); rank positional weight-based heuristic (Kao et al. 2011); Whale optimization algorithm (Jin et al. 2022). The only two studies that use constraint programming to solve the problem (Alakas et al. 2020; Alakaş 2021). When the results of the literature research given in Table 1 are examined, it can be easily seen that heuristic methods are often used to solve the RCALBP. Although exact methods such as mathematical programming have been used to solve the problem, the study using exact methods such as constraint programming, is still insufficient.

According to the literature research results mentioned above, this study focused on RCALBP with the following features: U-shape line, general case resource type, minimization of total cost, concurrent resource constraint type, and constraint programming solution method.

Studies in the literature where CP is used in the ALBP solution are given in Table 2. The first column of Table 2 shows the study, the line shape between the 2nd and 4th columns, the model type between the 5–6th columns, the objective function between the 7–12, and the last column show the additional characteristics. The literature will be examined in terms of this classification.

In the solution of ALBP, CP is mostly used for straight-line types. There are four studies that about U-shape (Bukchin and Raviv 2018; Mokhtarzadeh et al. 2021; Pınarbaşı 2021, 2022) and one two-sided (Kızılay and Çil 2020) ALBP study using CP as a solution method. There is a great need in the literature for studies to be carried out outside of straight assembly lines.

According to the number of models considered in the ALBP problem in the literature, there are two types of studies, single and mixed models. When the studies in Table 2 are examined, single-model ALBP was considered in most studies, and mixed-model studies are relatively few. Nevertheless, considering the different ALBP characteristics, it can be said that the use of CP in the single-model ALBP solution is still insufficient.

Table 2 The studies about CP and ALBP in the literature

Studies	Line shape			Model type		Objective function						Additional characteristics
	Straight	U-shape	Two-sided	Single	Mixed	Ns	C	Tw	Nr	Ms	Tc	
Bockmayr and Pisaruk (2001)	•			•		•						Combining integer programming method
Del Valle et al. (2003)	•			•		•						
Pastor et al. (2007)	•			•		•	•					
Topaloglu et al. (2012)	•			•		•						Rule-based modeling
Alağaç et al. (2013)	•			•			•					Stochastic task time
Pınarbaşı et al. (2016)	•			•			•					Stochastic task time
Öztürk et al. (2013)	•				•					•		Flexible assembly line
Öztürk et al. (2015)	•				•					•		Parallel assembly line
Alağaç et al. (2016)	•				•		•					
Bukchin and Raviv (2018)	•	•		•		•	•					Equipment selection problem
Pınarbaşı et al. (2019)	•			•			•					Assignment restrictions
Alakas et al. (2020)	•			•			•		•			Resource constraints
Pınarbaşı and Alakaş (2020)	•			•			•					Stochastic task time
Alakas and Toklu (2020)	•				•		•					Variable selection rules
Çil and Kizilay (2020)	•			•			•	•				Multi-manned assembly line
Kizilay and Çil (2020)			•	•		•		•				Multi-operator stations
Alakaş (2021)	•			•			•					Resource constraints
Pınarbaşı (2021)		•		•			•					Assignment restrictions
Pınarbaşı (2022)		•		•		•						Stochastic task time
Mokhtarzadeh et al. (2021)		•			•	•						Ergonomic risk
Stecke and Mokhtarzadeh (2022)	•			•			•					Ergonomic risk, human–robot collaboration
This study		✓		✓							✓	Resource constraints

Ns number of stations, *C* cycle time, *Tw* total workers, *Nr* number of resources, *Ms* makespan, *Tc* total station opening and resource usage costs

When the literature is evaluated in terms of the objective functions, it is seen that the number of stations and cycle time minimization were taken into account in most of the studies. In addition, total worker minimization (Çil and Kizilay 2020; Kizilay and Çil 2020), number of resource minimization (Alakas et al. 2020), and total completion time minimization (Öztürk et al. 2013, 2015) were used as objective functions. However, there is no study that takes into account the minimization of the station opening cost and the cost of resource usage simultaneously.

When CP studies in the literature are evaluated, there is no study dealing with the total cost minimization of single model U-shape ALBP. For this reason, U-type ALBP is taken into consideration in this study. Two new CP models using different methods for modeling resource constraints are proposed.

3 Problem definition and assumptions

In a production process, it may not always be sufficient to perform a task only by one operator. On the other hand, more than one resource may need to come together to fulfill the task. For example, considering a simple screwing operation, the task can be performed in the following ways: manually by only one operator, in combination with an operator and an automatic screwdriver, fully automatically by only one robot, or by any combination of these resources (e.g., cobot). These labor or machine required to perform a task is assumed as the resource in assembly line literature. Along with a task, the resources that achieve the task must also be assigned to the station. The problem in which the assignment of tasks and resources to the station is handled together is defined as the RCALBP (Ağpak and

Gökçen 2005). In the early versions of RCALBP, it was assumed that only one resource was used to accomplish a task i . In the developed version of the problem, alternative resource groups are used to perform a task. This problem type is defined as GRCALBP (Corominas et al. 2011). In this problem, it is assumed that different numbers of A, B, and C-type resources are used to perform a task i . For example, suppose task i can be performed using combinations of 3A, 2A and 2B or 3B and C resources. If task i is assigned to a station, one of these resource combinations must also be assigned to the related station. Otherwise, the task cannot be performed and the assembly process cannot be done.

The assumptions for RCALBP discussed in the study are assumed as follows:

- Each task is not divisible and should be assigned to a station.
- There is a precedence relationship restrictions between task pairs and these constraints should be satisfied in problem solving.
- Task times are predetermined deterministic constants.
- The cycle time is known and fixed.
- U-shaped line layout is considered.
- Numbers of different and alternative resource types have been taken into consideration.
- The number and types of references have been previously determined.
- Resources costs and station opening cost is known.
- Once a task is assigned to a station, the resources associated with that task must be assigned to that station.

4 Constraint programming models for U-GRCALBP

4.1 Overview of CP

This study is about the development of CP models in the solution of GRCALBP. CP is an effective problem-solving method used in the solution of many optimization problems such as scheduling, and timetabling in the literature (Gür et al. 2019).

The CP search algorithm produces solutions by using the decision variables, the domains of these variables and the constraints between these decision variables. In short, the search algorithm works as follows. First, the search algorithm determines the domain of each variable before it starts searching for a solution. It then propagates the constraints, reducing the domains of the variables that do not satisfy the constraints. This mechanism is called domain reduction. After this mechanism, a value is assigned to each decision

variable. If there is no variable that does not assign a value, all variables have taken values and the search is terminated. If there is at least one variable that does not assign a value, any variable is selected according to the variable selection rules. A value from the domain of the variable is selected for that variable and the selected value is assigned to the variable. After this stage, the domains of the variables are rearranged using the constraint propagation algorithm. Then it is checked whether there is a decision variable to be assigned value again. Similarly, the search process continues until there are no decision variables for which no value is assigned. After these stages, if there is an empty domain of any decision variables, backtracking mechanism is carried out to change the value of that variable. On the contrary, if there is no variable whose domain is empty, the search continues repeatedly. This search algorithm is continued until all decision variables are assigned feasible values and the search is terminated after the solution is reported. The methodological flowchart for CP approach is presented in Fig. 1 (Özder et al. 2021).

4.2 CP-1 model

Two different proposed constraint programming models are given in this section. In CP models, “or” logical operator is referred to define the alternative resource restrictions. Similarly, “and” operator is used to assign the resources together. These operators could be easily modeled in CP model by using generic form syntax. Likewise, the ability to easily model logical constraints is an important modeling advantage of CP. This advantage has provided great convenience in modeling alternative resource constraints in CP software. Necessary notations for models are given in Table 3. The proposed CP-1 model for U-GRCALBP is as follows:

Objective function:

$$\text{Min} \sum_{r=1}^R \sum_{j=1}^m \text{CR}_r \times v_{rj} + \text{CS} \times m. \quad (1)$$

Subject to:

$$\sum_{i=1}^N (x_i = j \vee x_i = 2m - j) t_i \leq \text{ct} \quad \forall j, \quad (2)$$

$$x_i \leq x_h \quad \forall (i, h) \in \text{Pr}, \quad (3)$$

$$\begin{aligned} & ((\alpha_{r1i} * (x_i = j) \leq v_{rj}) \vee (\alpha_{q1i} * (x_i = j) \leq v_{qj})) \\ & \wedge ((\alpha_{r2i} * (x_i = j) \leq v_{rj}) \vee (\alpha_{q2i} * (x_i = j) \leq v_{qj})) \\ & \dots \wedge ((\alpha_{rpi} * (x_i = j) \leq v_{rj}) \vee (\alpha_{qpi} * (x_i = j) \leq v_{qj})) \\ & \forall i, j, r, q, \end{aligned} \quad (4)$$

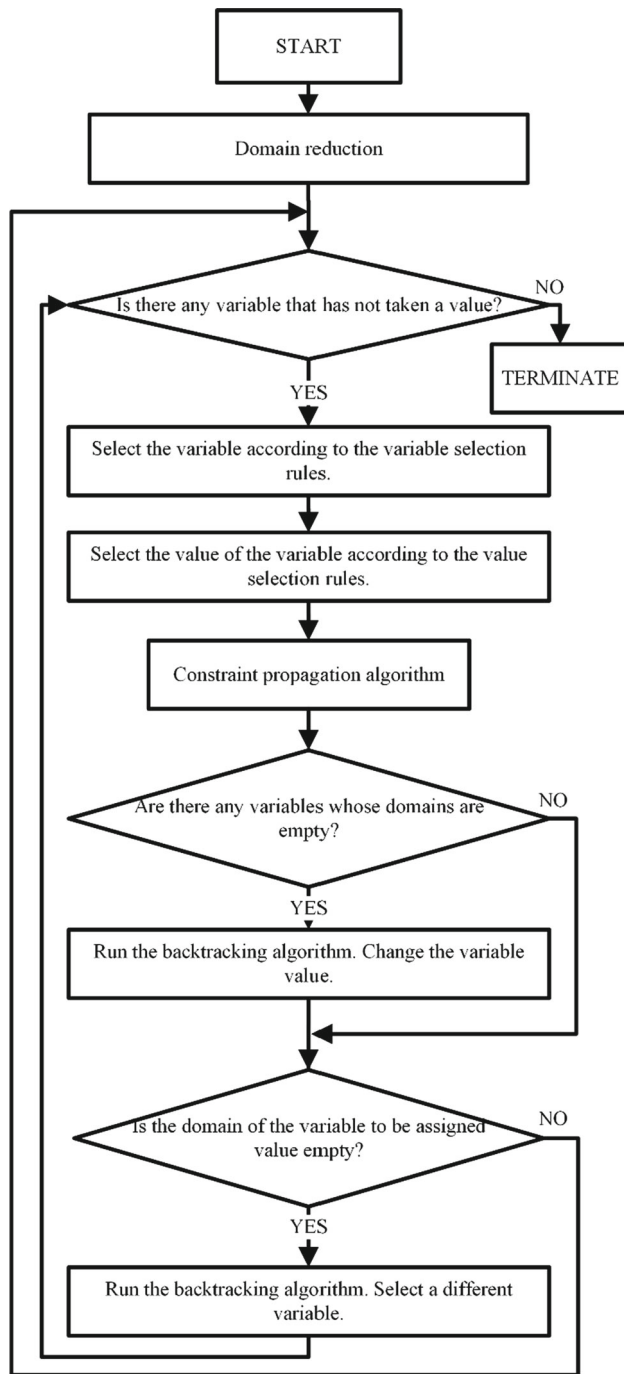


Fig. 1 Methodological flowchart of CP solution mechanism

$$x_i \in (1, \dots, s) \quad \forall i, \quad (5)$$

$$v_{rj} \in (0, \dots, \max(\alpha_{rpi})) \quad \forall i, p, r. \quad (6)$$

The objective function is the sum of the costs of the resources assigned to the stations and the station opening cost (Eq. 1). Equation 2 ensures that the total duration of the tasks assigned to the station does not exceed the cycle time. Equation 3 guarantees priority relationships. It should

be written for each priority relationship. Equation 4 takes into account resource constraints (Corominas et al 2011; Alakaş, 2021). If a task i is assigned to station j , it ensures that the resources needed to perform task i are assigned to the relevant station in desired amounts. With Eq. 5, the domain is defined for the decision variable that holds the station numbers to which the task i can be assigned. The decision variables' domains that keep the number of resources assigned to the station is defined by Eq. 6.

In CP models, decision variables can be desired to be equal to or greater than or less than a value. This logical query takes the value one if the expression is true and zero if not. Equality or inequalities are used in parentheses for logical inquiry in CP. For example, if x_i takes the value of j for the expression $(x_i = j)$ in the CP model, it returns one, in other cases, zero. Similarly, a similar query can be made by enclosing the smaller than or greater than expressions in parentheses.

4.3 CP-2 model

In the CP-2 model, resource constraints are changed and the model is formed as follows:

Objective function:

$$\text{Min} \sum_{r=1}^R \sum_{j=1}^m CR_r \times v_{rj} + CS \times m. \quad (7)$$

Subject to:

$$\sum_{i=1}^N (x_i = j \vee x_i = 2m - j) t_i \leq ct \quad \forall j, \quad (8)$$

$$x_i \leq x_h \quad \forall (i, h) \in \text{Pr}, \quad (9)$$

$$\begin{aligned} &(((x_i = j) \leq (v_{rj} \geq \alpha_{r1i})) \vee ((x_i = j) \leq (v_{qj} \geq \alpha_{q1i}))) \\ &\wedge (((x_i = j) \leq (v_{rj} \geq \alpha_{r2i})) \vee ((x_i = j) \leq (v_{qj} \geq \alpha_{q2i}))) \\ &\dots \wedge (((x_i = j) \leq (v_{rj} \geq \alpha_{rpi})) \vee ((x_i = j) \leq (v_{qj} \geq \alpha_{qpi}))) \\ &\forall i, j, r, q, \end{aligned} \quad (10)$$

$$x_i \in (1, \dots, s) \quad \forall i, \quad (11)$$

$$v_{rj} \in (0, \dots, \max(\alpha_{rpi})) \forall i, p, r. \quad (12)$$

As explained in the CP-1 model, the objective function is the minimization of the sum of resource usage and station installation costs (Eq. 7). Equation 8 is the cycle time constraint and Eq. 9 is the constraint of priority relationships. With Eq. 10, if a task i is assigned to station j , it ensures that sufficient resources required by the task are assigned to the relevant station (Corominas et al 2011; Alakaş, 2021). In Eqs. 11 and 12, the range of values that the decision variables can take is defined.

Table 3 Notations of the CP models

Parameters and indexes	
N	Number of tasks
R	Number of resources
P	Number of clauses
s	Number of stage $s = 2m - 1$
i, h	Task index ($i = 1, \dots, N$)
j	Station index
r, q	Resource index ($r, q = 1, \dots, R$)
p	Clause index ($p = 1, \dots, P$)
t_i	Processing time of task i
α_{rpi}	Number of resource units of type r in clause p of task i
ct	Cycle time
CR_r	Cost of the one unit of resource r
CS	A station opening cost
Pr	Precedence relations between tasks. If task i must be process task h immediately, it is shown as $(i, h) \in \text{Pr}$
Decision variables	
x_i	Stage number where task i is assigned to
m	Number of opened station
v_{rj}	Number of resources unit r that is assigned at station j

5 Illustrative example

In this section, the solution of the proposed model is explained through an illustrative example. The problem instance from Mete and Agpak (2013) is used as an illustrative example. The researchers solved this example as two-sided in that study. In this study, it is solved by assuming that it is a one-sided and U-type problem. Resource constraints are taken the same as in the study. Data on precedence relations, task processing times, and

Table 4 Data of the illustrative example

Task	Precedence	Task time	Resources
1	–	2	$(2A \vee B) \wedge (2A \vee C)$
2	–	3	$(A \vee B) \wedge (A \vee C)$
3	–	2	$5A \wedge (2B \vee 4C)$
4	1	3	$(A \vee 5B) \wedge (A \vee C)$
5	2	1	$(A \vee 5C) \wedge (B \vee 5C)$
6	3	1	$(4A \vee 4B) \wedge 5C$
7	4, 5	3	$(3A \vee 3B) \wedge (3A \vee 5C)$
8	5	3	$(5A \vee 4C) \wedge (5B \vee 4C)$
9	5, 6	2	$(A \vee 3B) \wedge (A \vee 3C)$
10	7, 8	2	$(A \vee 4C) \wedge (5B \vee 4C)$
11	9	2	$(5A \vee 2B) \wedge 3C$
12	11	1	$(4A \vee 4B) \wedge 4C$

tasks' resource needs of the problem are given in Table 4. Also precedence diagram of the illustrative example is given in Fig. 2. Resource costs are accepted as 12, 8, and 5 units for A, B, and C resources. Station opening cost is taken as 10 units. The cycle time is taken as 5.

Considering the data in Table 4, resource constraints related to tasks 1, 3, and 6 can be modeled as given in Eqs. 8, 9, and 10, respectively, for CP-1 model.

$$\left((2 \times (x_1 = j) \leq v_{Aj}) \vee (1 \times (x_1 = j) \leq v_{Bj}) \right) \wedge \left((2 \times (x_1 = j) \leq v_{Aj}) \vee (2 \times (x_1 = j) \leq v_{Cj}) \right). \quad (13)$$

$$(5 \times (x_3 = j) \leq v_{Aj}) \wedge \left((2 \times (x_1 = j) \leq v_{Bj}) \vee (4 \times (x_1 = j) \leq v_{Cj}) \right), \quad (14)$$

$$\left((4 \times (x_1 = j) \leq v_{Aj}) \vee (4 \times (x_6 = j) \leq v_{Bj}) \right) \wedge \left((5 \times (x_6 = j) \leq v_{Cj}) \right). \quad (15)$$

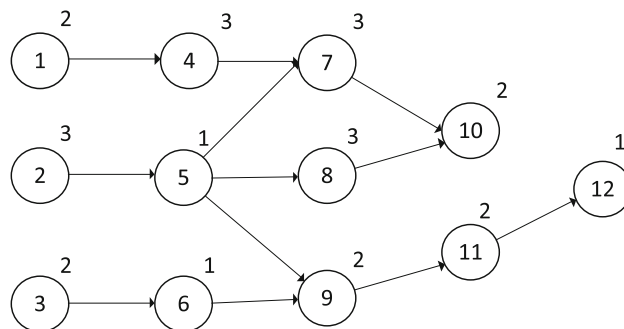
Unlike the CP 1 model, resource constraints for the above tasks are given as in Eqs. 11, 12 and 13 respectively for the CP-2 model.

$$\left(((x_1 = j) \leq (v_{Aj} \geq 2)) \vee ((x_1 = j) \leq (v_{Bj} \geq 1)) \right) \wedge \left(((x_1 = j) \leq (v_{Aj} \geq 2)) \vee ((x_1 = j) \leq (v_{Cj} \geq 2)) \right), \quad (16)$$

$$(x_3 = j) \leq (v_{Aj} \geq 5)) \wedge \left(((x_1 = j) \leq (v_{Bj} \geq 2)) \vee ((x_1 = j) \leq (v_{Cj} \geq 4)) \right), \quad (17)$$

$$\left(((x_1 = j) \leq (v_{Aj} \geq 4)) \vee ((x_6 = j) \leq (v_{Bj} \geq 4)) \right) \wedge \left(((x_6 = j) \leq (v_{Cj} \geq 5)) \right). \quad (18)$$

An example problem is solved with two CP models called as CP-1 and CP-2. The result of the CP-1 model and the CP-2 model are given in Table 5. In both models, the station number is five, and the total number of resources used by all stations is 29. The theoretical minimum station number is five, and the number of the station is obtained five with the two models. When the results are evaluated in terms of the number of stations, the optimum result has been reached with two CP models.

**Fig. 2** Precedence diagram of the illustrative example

6 Numerical experiments

6.1 Comparative results

Data sets from Alakas et al. (2020) are used to show the effectiveness of the proposed models in the experimental studies. While task times and priority relationships are considered to be the same as data sets, resource constraints have been generated by the authors for U-GRCALBP in a way that does not prevent the problem from reaching a feasible solution. It is assumed that there are 2 or 4 resource types in the data sets, and the numbers of tasks are range from 21 to 70 in the data set. Resource costs are taken as 12, 8, 5, and 10, and station opening cost is taken as 10. Both CP models are modeled and solved with ILOG Cplex Optimization v12.10. A PC with Intel Core™ i7, 1.30 GHz/1.7 GHz 64 bit processor and 8 GB of RAM are used to perform the models' solutions. The execution time limit is assumed 3600 s for both CP models. Numerical results reported according to the number of two and four resources are given in Tables 6 and 7. Since the problem addressed in the study is not discussed in another study in the literature, numerical results are given by comparing the proposed models. While making comparisons in the tables, performance criteria are highlighted as shown below. If one of the models is superior to the other in terms of the relevant criterion, that criterion is emphasized as stated.

Italic: Minimum number of stations.

Bold: Minimum number of resources.

Bold Italic: Minimum total cost.

Table 6 contains the comparative results of problem sets with two resource types. When the models' results are evaluated in terms of the minimum number of stations, it can be said that the CP-1 model has better results in two problem sets and the CP-2 model has better in one problem set. In most of the problem sets, both models have reached the same station number value. When the number of resources obtained is evaluated, it can be said that the CP-2 model obtains the minimum number of resources in three problem sets. However, in general, solutions with the same

number of resources have been produced in both models. It cannot be said that both models establish a clear superiority to each other in total cost results for two resource cases.

The results of the problem sets with four resource types are reported in Table 7. When the results are evaluated according to the criteria of the number of stations, both models showed similar performance. Similarly, considering minimizing the number of resources used, CP-2 model is better than CP-1 model in seven problem sets. CP-1 model is also better in four problem sets. However, considering the total cost criteria, it is seen that the CP-2 model is superior to the CP-1 model. CP-2 model are better in eight problem sets than CP-1 and are equal to eight problem sets to the CP-1 model.

Table 8 shows the number of problems where both models provide superiority to each other according to each performance criterion. It is easily seen in the results that the more the number of resources, the more obvious the superiority between the models. While both models show similar performance in problems with two resource types, it is seen that the CP-2 model performs better than the criterion of minimizing the total cost in problems with four resource types.

Some remarkable results are also obtained in numerical results. Considering the Tongue $c = 196$ problem in Table 6, while the results of the CP-1 model are $m = 19$, the total number of used resources is 97, and the total cost is 1122, for the CP-2 model, these values are 21, 94, and, respectively. The total cost is reported as 1114. More stations are opened with the CP-2, and fewer resources are used, but it achieved a low-cost result. In problem sets balanced with an equal number of stations (e.g. Sawyer $c = 31$, Kilbridge $c = 92$ and Tongue $c = 196$ for four resources type), the line can be balanced with a lower number of resources and lower cost. These situations show a trade-off between the number of opened stations and the number of resources to reach the minimum cost. However, it depends on the given station opening and resource usage costs, and resource constraints.

Table 5 The illustrative example solution results

CP-1				CP-2			
Station	Assigned Tasks	Station time	Resource type (#)	Station	Assigned Tasks	Station time	Resource type (#)
1	2, 3	5	A(5), B(2)	1	2, 3	5	A(5), B(2)
2	10, 11, 12	5	B(4), C(4)	2	10, 11, 12	5	B(4), C(4)
3	1, 4	5	A(2)	3	1, 4	5	A(2)
4	5, 6, 8	5	B(4) C(5)	4	5, 6, 8	5	B(4) C(5)
5	7, 9	5	A(3)	5	7, 9	5	A(3)

Table 6 Two resources case experiments' results

Problem set	# tasks	Cycle time	CP-1			CP-2			Traditional U type		
			# stations	# Used resources	Total cost	# stations	# used resources	Total cost	# stations	# used resources	Total cost
Mitchell	21	14	8	44	520	8	44	520	8	47	544
		18	6	34	404	6	34	404	6	38	444
		25	5	31	354	5	31	354	5	35	410
		35	3	24	274	3	24	274	3	26	298
Heskiaoff	28	110	10	45	540	10	45	540	10	63	716
		138	8	38	448	8	38	448	8	56	644
		205	6	30	348	6	30	348	5	41	458
		324	4	23	256	4	23	256	4	35	388
Sawyer	30	25	14	67	780	14	67	776	14	75	868
		31	12	55	652	12	55	652	11	68	786
		37	10	46	544	10	46	544	9	59	670
		47	8	41	472	8	41	472	7	51	570
Kilbridge	45	55	<i>11</i>	56	658	12	56	668	11	80	906
		69	9	48	558	9	48	558	8	67	756
		92	7	39	446	7	39	446	6	55	620
		110	6	35	400	6	34	400	6	47	532
Tongue	70	196	<i>19</i>	97	1122	21	94	1114	18	125	1416
		294	13	72	818	13	72	830	12	97	1076
		391	11	57	662	<i>10</i>	56	640	9	75	834
		502	8	48	540	8	48	540	7	62	682

When the proposed CP models are evaluated in terms of solution time, the results obtained are given in Table 9. It can be said that the CP-2 model is relatively better in terms of average CPU time for problem sets with two resources. When the maximum, minimum, and standard deviation values are examined, it can be said that both models require a long solution time for solving the problem sets with two resources. Both models could not obtain the optimum solution in less than the solution time limit for all problem sets with four resources.

Traditional U-type model results are given in Tables 6 and 7. When the results are evaluated in general, it can be said that the proposed CP models are effective in solutions to the problem. According to the total cost and resource numbers, both CP models' results are lower than traditional U-type model results for all problem sets. However, the CP models may have higher station numbers than traditional U-type model due to resource constraints. The CP-2 model performs better in solving the problem while increasing the number of resource types and tasks.

The comparative results of the theoretical number of stations obtained on a traditional U-type line model with the results given in Tables 6 and 7 are given in Table 10. The purpose of this comparison is to evaluate whether

resource constraints cause a significant increase in the number of stations. The gap value reported in the table is given in Eq. 19. According to the results reported in Table 8, the biggest gap value Tongue $c = 391$ is obtained in two resource-constrained problems. The smallest gap is obtained as 0.00 in problem sets where the theoretical cycle time and the number of stations obtained in many problems are the same. Mean gap values are obtained as 7.47% and 7.83%, respectively, for the problems with two and four resource types for the CP-1 model, while 7.89% and 7.83% for the CP-2 model. These values show that the number of stations obtained with both proposed models is acceptable according to the theoretical number of stations obtained with the traditional U-type line model.

$$\%gap = \frac{(\text{Result of proposed model} - \text{Theoretical \#station})}{\text{Result of proposed model}} \times 100. \quad (19)$$

Considering all these results, managers should make the resources used for the tasks as common as possible to establish the line more effectively. Thus, the assembly line will be established by evaluating more assignment alternatives. At the same time, the number of resource types

Table 7 Four resources case experiments' results

Problem set	# Tasks	Cycle time	CP-1			CP-2			Traditional U type		
			# stations	# Used resources	Total cost	# stations	# used resources	Total cost	# stations	# used resources	Total cost
Mitchell	21	14	8	42	364	8	42	364	8	45	399
		18	6	34	290	6	34	290	6	34	324
		25	5	30	260	5	30	260	5	39	341
		35	3	22	175	3	22	175	3	29	261
Heskiaoff	28	110	11	44	450	11	45	450	10	59	599
		138	8	38	373	8	36	368	8	54	520
		205	6	29	295	6	29	295	5	41	364
		324	4	26	236	4	26	236	4	32	295
Sawyer	30	25	15	71	655	15	66	649	14	78	736
		31	12	55	554	12	57	561	11	70	705
		37	10	50	489	10	50	494	9	72	653
		47	8	44	419	8	44	419	7	63	527
Kilbridge	45	55	11	61	586	11	61	578	11	83	772
		69	9	50	494	9	54	495	8	69	666
		92	7	46	426	7	42	418	6	58	553
		110	6	37	367	6	39	371	6	59	521
Tongue	70	196	19	110	985	19	105	938	18	129	1161
		294	13	86	729	13	75	678	12	113	979
		391	10	70	584	10	66	565	9	88	770
		502	8	60	494	8	55	481	7	70	619

Table 8 Summary results based on the performance measurements

# Resource type	Model	Min # stations	Min # resources	Min total cost
2	CP-1	2	–	2
	CP-2	1	3	3
4	CP-1	–	4	4
	CP-2	–	7	8

Table 9 CPU time comparison of the proposed models

# Resource type	Model	Mean	Max	Min	Std. dev
2	CP-1	2734.15	3600	1.43	1540.37
	CP-2	2726.76	3600	1.69	1553.10
4	CP-1	3600	3600	3600	0
	CP-2	3600	3600	3600	0

needed can be reduced by collecting resources. Thus, the solution to the problem will be more straightforward.

6.2 Managerial implications

In this section, managerial implications for professionals, organizations, and society will be discussed using results from numerical experiments. The effects of model

parameters on line performance in practice are presented. In this context, the following managerial implications can be suggested to production managers.

- Managers can easily examine the effects of different resource types and various combinations of these resource types on line performance.
- Evaluation of alternative resource combinations provides decision support to managers in the selection of appropriate resources.
- The tradeoff between performance parameters such as number of stations, number of used resources and total cost can be analyzed.
- The proposed models allow managers to create a more effective workforce, resource capacity and production plans.

Table 10 Comparison of results by number of stations

Problem set	# tasks	Cycle time	Theoretical # station	Two resources				Four resources			
				CP-1	%gap	CP-2	%gap	CP-1	%gap	CP-2	%gap
Mitchell	21	14	8	8	0.0	8	0.0	8	0.0	8	0.0
		18	6	6	0.0	6	0.0	6	0.0	6	0.0
		25	5	5	0.0	5	0.0	5	0.0	5	0.0
		35	3	3	0.0	3	0.0	3	0.0	3	0.0
Heskiaoff	28	110	10	10	0.0	10	0.0	11	9.1	11	9.1
		138	8	8	0.0	8	0.0	8	0.0	8	0.0
		205	5	6	16.7	6	16.7	6	16.7	6	16.7
		324	4	4	0.0	4	0.0	4	0.0	4	0.0
Sawyer	30	25	13	14	7.1	14	7.1	15	13.3	15	13.3
		31	11	12	8.3	12	8.3	12	8.3	12	8.3
		37	9	10	10.0	10	10.0	10	10.0	10	10.0
		47	7	8	12.5	8	12.5	8	12.5	8	12.5
Kilbridge	45	55	10	11	9.1	12	16.7	11	9.1	11	9.1
		69	8	9	11.1	9	11.1	9	11.1	9	11.1
		92	6	7	14.3	7	14.3	7	14.3	7	14.3
		110	5	6	16.7	6	16.7	6	16.7	6	16.7
Tongue	70	196	18	19	5.3	21	14.3	19	5.3	19	5.3
		294	12	13	7.7	13	7.7	13	7.7	13	7.7
		391	9	11	18.2	10	10.0	10	10.0	10	10.0
		502	7	8	12.5	8	12.5	8	12.5	8	12.5

- Managers have the opportunity to eliminate resource types that do not affect line performance.
- Managers may have the opportunity to choose the most suitable one for their line evaluation from the proposed CP models.
- Although CPU time increases as the problem size grow, effective and efficient results can be presented to managers in a short time limit such as one hour.

7 Conclusion and future research directions

In this study, two innovative and effective exact modeling approaches are presented for the resource-constrained U-shaped assembly line balancing problem. General and concurrent resource constraints are considered as resource constraint types. The proposed models aim to minimize the sum of the station opening cost and the costs of the resources used. Two different CP models based on different modeling of resource constraints are proposed to solve the problem. Although constraint programming is a new modeling technique for the solution to the ALBP in the literature, it is a frequently used method for solving

combinatorial problems such as scheduling, assignment problems, and car sequencing.

The performances of the proposed models are tested with 20 literature problems. While task times and priority relations are preserved in the literature problems, resource constraints have been produced by the authors with different reference numbers. In addition to the total cost, the number of stations obtained, the number of resources, and CPU time are also considered as performance criteria. According to the numerical experimental results, the proposed models showed a remarkable performance in solving the problem. Although it can be said that both models show similar performance in general, the CP-2 model is more superior in terms of obtaining the minimum total cost with the increase in the number of resources. The models performed similarly in terms of CPU time. However, with the increase in the number of resources, the time needed to solve the problem also increases. Besides these results, it has been shown that model solutions cause interesting trade-offs among performance criteria. Both models showed notable performance in comparison with the theoretical number of stations for the traditional U-type model.

There are some limitations in this study in terms of features of ALBP. However, these limitations can be easily

overcome by various future research directions. One of these limitations is that this study considers the U-type line configuration. So, proposed CP models can be developed for different line configurations (e.g. parallel, two-sided etc.) with different number of resource types. Another limitation of this study is that task times are considered deterministic. Therefore ALBP, where task times are stochastic, would also be a notable future study. In this study, datasets with a task number between 21 and 70 are solved. Developing heuristic methods to solve large datasets or large real-life problems would be promising future work. Moreover, it will be a very innovative future work to develop models in which the total cost will be minimized for the solution of ALBP, which uses Industry 4.0, the internet of things, and augmented reality-based resources.

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Declarations

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